

Article **An Investigation into the Optimal Dimple Geometry in a Single-Dimple Sliding Contact**

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Abstract: This study analyzes the influence of nine distinct texture geometries on a convergent oil film gap using a simulation model. The geometrical dimensions of the textures are characterized by the texture area density, $S_{tx, A}$ and the ratio of the textured-to-untextured area $(A_{tx, A})$. The results show that different texture geometries optimize the tribological performance depending on the value of *Stex*.,*A*. Rectangular textures with variable widths (85% of the texture length *atex*.) significantly enhance lifting and the drag force across a broad range of *Stex*.,*A*. Furthermore, rectangular textures with a constant width (85% of the global width b_0) show the best improvement within this study. The investigation also reveals that a small texture pitch angle, *αtex*, further enhances tribological performance.

Keywords: textures; single dimple; full film lubrication; CFD

1. Introduction

In [\[1\]](#page-13-0), it is presented that reducing the viscosity by 1 mPas at a temperature of 150 $^{\circ}$ C can lead to potential fuel savings ranging from 0.8% to 4%. The actual amount of savings will vary depending on the engine and test cycle. According to Woydt [\[1\]](#page-13-0), Germany could save over 1.64 megatons of $CO₂$ per year by implementing a conservative fuel-saving potential of 1%. As a result, many researchers are focusing on the use of low-viscosity oils. In general, decreasing the viscosity also reduces the hydrodynamic pressure for constant oil film gap heights, which can be avoided by applying surface textures, as explained by Grützmacher et al. [\[2\]](#page-13-1), who published that increasing the hydrodynamic pressure is one working principle of surface texturing. The concept of surface modifications has been under consideration for decades, particularly in the context of piston rings on cylinder liner contacts, as presented among others in [\[3\]](#page-14-0), or for micro-grooved journal bearings [\[4\]](#page-14-1). The research effort, presented through the number of publications, for the application of surface textures strongly increased in the past 25 years [\[5](#page-14-2)[–8\]](#page-14-3). The application of textures in hydrodynamic contacts can enhance the load-carrying capacity, as highlighted in [\[7](#page-14-4)[,9\]](#page-14-5). To apply this beneficial behavior, various manufacturing processes are available for creating texture geometries, as summarized by Coblas et al. [\[10\]](#page-14-6):

- Adding material technologies;
- Removing material technologies;
- Material displacement technologies;
- Self-forming methods.

Typical examples of adding material technologies include the chemical and physical deposition processes, which are used in [\[11\]](#page-14-7) to create micro-frustum-shaped dimples with a diameter of 50 μ m to 75 μ m on the base area. Laser surface texturing and mechanical processes, e.g., grinding and honing, are examples of removing material technologies. In [\[12\]](#page-14-8), cylindrical-shaped dimples with a radius of up to 5 μ m were created by a laser,

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and it was observed that the geometry of the texture was strongly influenced by the laser's parameters. Pettersson et al. [\[13\]](#page-14-9) developed a process for manufacturing embossing tools, which they used to produce pyramid- and rooftop-shaped textures. This method is an example of a material displacement technology. Self-forming texture dimples were numerically analyzed in [\[14\]](#page-14-10), where the texture was created through elastic deformation caused by the applied load. Consequently, the shape of the texture depends on the load and the stiffness of the system.

The manufacturing process itself can limit the texture geometry. Nevertheless, the shape of the texture geometry varies in many publications, and in [\[15–](#page-14-11)[22\]](#page-14-12), the influence of the texture geometry is analyzed in detail. In [\[15,](#page-14-11)[17–](#page-14-13)[20\]](#page-14-14), different texture shapes for a parallel oil film gap were evaluated using the Reynolds equation. Since the oil film gap is rarely parallel in technical applications, this study investigates the performance of different texture geometries for a convergent oil film gap. Regarding the simulation methodology, Dobrica et al. [\[23\]](#page-14-15) published that the application of the Reynolds equation in full film lubrication is valid for large enough dimple aspect ratios and low Reynolds numbers. Simulating transient elastohydrodynamic contacts using the Reynolds equation results in small deviations compared to the simulating fluid dynamic models [\[24\]](#page-14-16). This study employs a full film lubrication model, incorporating Stokes flow in the simulation.

Wei et al. [\[21\]](#page-14-17) analyzed different texture shapes on a convergent oil film gap, where the texture had specific dimensions. This led to different texture area densities $S_{tx, A} = A_{tx} / A_0$, as the texture area *Atexture* depends on the texture shape (cf. Figure [1\)](#page-1-0). Furthermore, they compared the performance of the different texture geometries by using a constant number of dimples; consequently, the texture area density $S_{tex, t}$ for every textured surface is different [\[21\]](#page-14-17). Summarized, different texture area densities *Stex*.,*^A* were examined.

Figure 1. Overview of different texture geometries (unscaled). **Figure 1.** Overview of different texture geometries (unscaled).

In contrast to them, Uddin et al. [\[17\]](#page-14-13) investigated different texture geometries at a constant texture area density $S_{textrm{tex}}$. Additionally, they analyzed the influence of the bottom profile, which was flat, curved or coned [\[17\]](#page-14-13). In [\[18\]](#page-14-18), five different texture densities $S_{texA, A}$, in the range between 3% and 30%, were analyzed for a parallel sliding contact. Kumar et al. [\[19\]](#page-14-19) analyzed eight different texture shapes and compared their load-carrying capacities over the texture area density *Stex*.,*^A* for a thrust bearing. In [\[20\]](#page-14-14), the dimensionless average pressure was analyzed for three different texture shapes, including the influence of the texture area density $S_{tx, A}$. In contrast to these studies focusing on a parallel oil film gap, this study will discuss the influence of texture shape on a convergent oil film gap for

As mentioned in [\[17\]](#page-14-13), different bottom profiles influence the tribological performance, and it is found that a single wedge significantly enhances the tribological performance in full film lubrication. In [\[22,](#page-14-12)[25\]](#page-14-20), the performance of a wedge-shaped texture was analyzed in mixed lubrication and it could be observed that this texture improves tribological performance.

Based on the past paragraphs, this raises the question of the influence of the texture geometry at a constant *Stex*.,*^A* and of the pitch angle *αtex*. . A pitch angle *αtex*. equivalent to zero can be achieved with a constant texture height *h*, otherwise α_{text} is >0[°].

2. Methodology

2.1. Simulation Methodology

specific texture area densities *Stex*.,*A*.

Marian et al. [\[8\]](#page-14-3) published that, in about 27% of all publications in the field of surface texturing between 1990 and 2020, a simulation model was investigated, and about 37% focused on hydrodynamic lubrication. In [\[15](#page-14-11)[,17–](#page-14-13)[20\]](#page-14-14), the Reynolds equation is solved, which has strict limitations regarding the texture geometry and Reynolds number [\[23\]](#page-14-15). To avoid these problems in this current work, a Stokes flow is used. Cupillard et al. [\[26\]](#page-14-21) discussed the influence of inertia effects in textured hydrodynamic contacts, mentioning that for low Reynolds numbers, these effects are neglectable. For the geometry used in this study, the maximal Reynolds number is approximately $Re \approx 1.6$ and, therefore, the inertia effects, which are described by the nonlinear term of the Navier–Stokes equation, are neglected. Based on these results, the application of the Stokes flow is acceptable. Equations (1) and (2) present the multiphase Stokes flow and the continuity equation, which is necessary to calculate the velocity field \vec{u} and pressure field *p*. Here, *v* is the kinematic viscosity, ζ is \rightarrow

the second viscosity, I is the identity matrix, ρ is the density and f is the body force. This multiphase flow has to be solved if cavitation occurs; that means that the minimal pressure p_{min} is lower than the vapor pressure p_v . Otherwise, the single-phase flow, presented by Equation (3), can be solved. In the case of cavitation, the viscosities *ν*, *ζ* and density *ρ* become scalar fields. The second viscosity *ζ* is set equal to the kinematic viscosity *ν*, satisfying the inequality presented in [\[27\]](#page-14-22). In [\[28\]](#page-14-23), this assumption was compared with an already existing solver for a multiphase flow.

$$
-\nabla \cdot \left\{ v \left[\nabla \vec{u} + \left(\nabla \vec{u} \right)^T - \frac{2}{3} \left(\nabla \cdot \vec{u} \right) I \right] + \zeta \left(\nabla \cdot \vec{u} \right) I \right\} + \nabla p = \rho \vec{f} \tag{1}
$$

$$
-\nabla \cdot \vec{u} = 0 \tag{2}
$$

$$
-\nu \Delta \vec{u} + \nabla p = \rho \vec{f} \tag{3}
$$

In [\[29\]](#page-14-24), the Merkle [\[30\]](#page-14-25) cavitation algorithm was used to simulate a journal bearing. This cavitation algorithm is described by Equations (4)–(9) and is based on a transport partial differential equation (cf. Equation (4)), where α_v represents the vapor volume fraction (cf. Equation (7)) and m^+ and m^- are the source terms that describe the condensation and vaporization processes. The vapor volume fraction α_v represents the portion of vapor volume V_v in the complete volume $V_v + V_l$. Therefore, the sum of the vapor volume fraction α_v

and liquid volume fraction α_l is 1. The condensation term \dot{m}^+ depends on the condensation constant *Cc*, the density of the fluid ρ_l and vapor ρ_v , the reference time t_{∞} and speed U_{∞} and the liquid volume fraction α_l . The vaporization rate m^- depends on the parameter mentioned earlier and the vaporization constant *Cv*. The density *ρ*—and viscosity field *ν* are presented in the case of cavitation by multiplication, as shown in Equations (8) and (9).

$$
\nabla \cdot \left(\vec{u} \alpha_v\right) = \dot{m}^+ - \dot{m}^- \tag{4}
$$

$$
\dot{m}^+ = Cc \frac{\rho}{\rho_l \rho_v} \frac{(1 - \alpha_l)}{0.5 U_{\infty}^2 t_{\infty}} \text{max}(p - p_v, 0)
$$
\n⁽⁵⁾

$$
\dot{m}^{\dagger} = Cv \frac{\rho}{\rho v^2} \frac{\alpha_l}{0.5U_{\infty}^2 t_{\infty}} \max(p_v - p, 0)
$$
\n(6)

$$
\alpha_v = \frac{V_v}{V_v + V_l} \tag{7}
$$

$$
\rho = \rho_v \alpha_v + \rho_l (1 - \alpha_v) \tag{8}
$$

$$
\nu = \nu_v \alpha_v + \nu_l (1 - \alpha_v) \tag{9}
$$

To solve these equations numerically, the finite element method FEM is applied using a Python-based simulation package called Netgen/NGSolve [\[31\]](#page-14-26). For this study, the steady state is of interest, so the time derivatives for the transport and Stokes equation are not considered. For discretization of the geometries, tetrahedral-shaped elements with secondorder shape functions are used. A maximal mesh size of $25 \mu m$ was defined to achieve sufficient accuracy. This mesh size was determined through a mesh study, where deviations of less than 0.5% for lifting and the drag force were observed.

Table [1](#page-3-0) presents the simulation parameters for the oil and cavitation algorithm based on the work presented in [\[32,](#page-14-27)[33\]](#page-15-0).

Table 1. Simulation parameters.

Parameters	
Density oil liquid ρ_l	860 kg/m^3
Density oil vapor ρ_v	0.13 kg/m^3
Dynamic viscosity liquid η_l	130 mPa s
Dynamic viscosity vapor η_v	0.02 mPa s
Condensation coefficient C_C	33.3
Vaporization coefficient C_v	0.00155
Vapor pressure p_v	165 Pa
Input velocity U_{∞}	5 m/s
Reference time t_{∞}	l_0/U_∞

In [\[28\]](#page-14-23), this self-developed simulation methodology is compared with the results of the existing OpenFOAM IntherphaseChangeFOAM [\[34\]](#page-15-1) solver, which is based on the full Navier–Stokes equation.

2.2. Texture Geometries and Simulation Parameters

The texture height at the inlet, $h_{text,lin}$, was set to 30 μ m and was kept constant in this work. Figure [1](#page-1-0) shows the smooth convergent oil film gap and nine different texture geometries. The different dimple geometries were selected based on two points of view. On the one hand, as few as possible parameters should be varied, and on the other hand, these geometries should be quite simple so that a potential manufacturing process is applicable. To evaluate the performance of specific texture shapes, the texture area density $S_{texA} = A_{texA} / A_0$ is used. This means that a specific texture area density $S_{texA} A$ is defined, and with the help of the equations presented in Figure [1,](#page-1-0) the geometrical parameter *atex*. is calculated. The parameters of the smooth wedge are $l_0 = b_0 = 2$ mm, $h_0 = 15$ µm and

 $\alpha_0 = 0.15^{\circ}$. For the rectangle with a constant width, the texture width was defined as 85% of *l*₀. This 85% result is the best tribological performance in [28]. [The](#page-14-23) angle α_{Chev} is set to 20°. Initially, the tribological performance of the different texture geometries was analyzed for a constant texture height $h_{textrm{tex}} = h_{textrm{tex}} = 30 \mu m$, which corresponds to a pitch angle of $\alpha_{tex} = 0^\circ$. For analyzing the influence of the pitch angle α_{tex} , the texture height at the outlet was varied between 0 and 30 μ m with a s step size of 5 μ m. This resulted in different pitch angles of the texture *αtex*. . she angles of the texture μ .

with the help of the equations presented in \mathcal{L}_max and \mathcal{L}_max

In Figure [2,](#page-4-0) the boundary conditions for an exemplary rectangle-shaped texture are In Figure 2, the boundary conditions for an exemplary rectangle-shaped texture are depicted. The bottom surface of the oil film gap is moving with the velocity <u>u</u>, while the top surface of the oil film gap and the surface of the texture are stationary. The lateral surface of the oil film has a relative pressure of $p = 0$ Pa, resulting in a liquid volume fraction of $\alpha_l = 1$. For all other boundary conditions not mentioned, a Neumann boundary condition, zero gradient, is applied. Furthermore, it is assumed that all surfaces are completely smooth. In Figure \angle , the boundary conditions for an exemplary rectangle-shaped textu

Figure 2. Boundary conditions for a textured oil film gap (unscaled). **Figure 2.** Boundary conditions for a textured oil film gap (unscaled).

For the numerical implementation of the simulation model, the sparse direct solver For the numerical implementation of the simulation model, the sparse direct solver Unsymmetric Multi Frontal Package UMFPACK was used. Unsymmetric Multi Frontal Package UMFPACK was used. $\frac{1}{2}$ solving the previously discussed equations leads to a previous to a previous field $\frac{1}{2}$ and a velocity \frac

Solving the previously discussed equations leads to a pressure field *p* and a velocity field *u* for each geometry. In postprocessing, the lifting force $\overrightarrow{F}_{lift}$ is calculated by integrating the pressure field over the bottom surface (cf. Equation (10)). The drag force $\overrightarrow{F}_{drag}$ is calculated by integrating the shear stresses τ_x over the bottom surface.

$$
\overrightarrow{F}_{lift} = \int_A p_{(x,y,z=0)} \cdot \overrightarrow{n} dA \tag{10}
$$

Both forces, calculated on a smooth convergent oil film gap, were compared with the analytical solution according to [\[35\]](#page-15-2), and similar results could be achieved.

In general, the texture should increase the lifting force $\overrightarrow{F}_{lift}$, decrease the drag force $\overrightarrow{F}_{drag}$ or combine both. However, to combine these two parameters, the performance enhancement ratio (PER), which is published in [\[36\]](#page-15-3), is used. Sharma et al. [\[36\]](#page-15-3) used the load-carrying capacity and friction coefficient as parameters. In this study, the ratio of the magnitudes of the lifting forces between textured $\Big\vert$ $\overline{}$ $\left| \overrightarrow{F}_{lift,textured} \right|$ and untextured $\overline{}$

$$
\begin{vmatrix}\n\overrightarrow{F}_{lift,untextured} & \text{geometries is divided by the ratio of the magnitudes of their respective\ndrag forces $\overrightarrow{F}_{drag, \text{texured}} \mid$ and $\overrightarrow{F}_{drag,untextured} \mid$ (cf. Equation (11)).\n
$$
\overrightarrow{F}_{lift, \text{textured}} \mid
$$
\n
$$
PER = \frac{\overrightarrow{F}_{lift,untextured}}{\overrightarrow{F}_{drag, \text{texured}} \mid}
$$
\n(11)
$$

3. Results *3.1. Influence of Texture Geometry for Constant Width*

3.1. Influence of Texture Geometry for Constant Width

In Figure [3,](#page-5-0) the performance enhancement ratio (PER) over the texture area density S_{tex} ,*A* for each geometry is depicted. The maximal texture area density S_{tex} ,*A* for every geometry is different, as the texture should not protrude the convergent oil film gap's base area. In regions of low texture area density $S_{tex, A}$ (less than 30%), the rectangle with a variable width and chevron-shaped texture led to the best tribological performance. In the region of a texture area density between 30% and 70%, the rectangle with a variable width region of a texture causes the highest performance enhancement ratio (PER). With a further increasing texture causes the rectangle with a constant width and the rectangle with a constant width and the rectangle with a constant width and the r area density, the performance of the rectangle with a constant width achieves the highest
PER, in contrast to the this where PER, in contrast to the regions with a low texture area density $S_{tex, A}$, where this geometry has the worst tribological performance. As the texture area density $S_{tex, A}$, where this geometry has the worst tribological performance. As the texture area density $S_{tex, A}$ increases, the difference by a continuous increases, \mathbf{r} denotes difference between both half hexagons increases, followed by a continuous decrease. In the ancience between both half hexagons increases, to
howed by a continuous decrease. In the observed region, the half hexagon leads to better tribological performance compared to observed region, the name modigion relats to better inborogieal performance compared to the half hexagon (inlet large), which is positioned so that the large area is located on the inlet side. Potentially, with increasing texture area density $S_{tex,A}$ this effect can be reversed.
Furthermore, it is depicted that in regions of texture area densities S_{max} less than 40%, the Furthermore, it is depicted that in regions of texture area densities *Stex*.,*^A* less than 40%, the Fundatively it is depicted that in regions of texture area densities $\mathcal{S}_{\text{RIX},A}$ ress than 10%, the square, the equilateral triangle and the hexagon exhibit similar tribological behaviors. The behaviors are equinited a margin and the deluged countries similar and seguent conditions. The half hexagon (inlet large) and the semicircle led to tribological performance in a similar manner. $\frac{1}{10}$ lie han hexagon (nuet large), which is positioned so that the large area is located on the $f(x) = \frac{1}{2} \int_0^x f(x) \, dx$

Figure 3. Performance enhancement ratio over texture area density for constant width $h_{tex, out} = h_{tex, in} = 30$ m.

In Figures [4](#page-6-0) and [5,](#page-6-1) the magnitudes of the lifting force $\Big|$     are depicted. It can be observed that all textures increase the hydrodynamic pressure *p*, $\left| \overrightarrow{F}_{lift} \right|$ and drag force $\left| \overrightarrow{F}_{drag} \right|$ which leads to a rising lifting force $\overrightarrow{F}_{lift}$. Additionally, the friction force $\overrightarrow{F}_{drag}$ decreases. However, the performance enhancement ratio (PER) of the chevron-shaped texture does not provide the highest values, although the magnitude of the drag force $\Big\vert$   lowest. In contrast, the semicircle and half hexagon (inlet large) texture result in the highest → *Fdrag* $\overline{}$ is the drag force $\overline{}$ $\overline{}$ $\overline{}$ \vert $\overrightarrow{F}_{drag}$. Generally, for the texture area densities $S_{tex,AA}$ less than 30%, the drag $\overline{}$ force $\begin{array}{c} \begin{array}{c} \begin{array}{c} \end{array} \\ \begin{array}{c} \end{array} \end{array} \end{array}$ ļ $\left| \vec{F}_{drag}\right|$ does not differ much between the different geometries. The maximal lifting \vert force $\bigg|$ $\overline{}$ $\overline{}$ \vert $\overrightarrow{F}_{lift}$ is achieved before the maximal performance enhancement ratio (PER), as the

influence of decreasing friction also positively affects tribological performance. However, with the further increasing texture area density $S_{textrm{\tiny{tex}}A}$, the decreasing lifting forces $\Big\vert$ dominate, leading to a decrease in the performance enhancement ratio (PER). For the $\left| \vec{F}_{lift} \right|$ abilitative, relating to a decrease in the performance enhancement ratio (FER). For the triangle, half hexagon, hexagon and semicircle textures, this behavior is not visible, as the geometry dimension is limited by the assumption that the texture cannot protrude the convergent oil film gap. liftimative of $\ddot{}$ σ is achieved before the maximal performance enhancement ratio (PER), σ aonmia
. . . . (PER). For the triangle, half hexagon, hexagon and semicircle textures, this behavior is not

lowest. In contrast, the semicontrast, the semicontrast, the semicontrast, the high-

Figure 4. Lifting force over texture area density for constant texture width $h_{tex, out} = h_{tex, in} = 30$ m.

Figure 5. Drag force over texture area density for constant texture width h **Figure 5.** Drag force over texture area density for constant texture width $h_{textrm{text},out} = h_{textrm{text},in} = 30$ m.

3.2. Influence of Pitch Angle

³.
Since the texture height is small compared to its horizontal and vertical extents, the Since the texture height is small compared to its horizontal and vertical extents, the pitch angle α_{tex} is not used directly in this case. Instead, the texture height on the outlet side $h_{textrm{text,}out}$ is used as a varying parameter.

In Figure [6,](#page-7-0) the texture area density $S_{tex,A}$ is plotted over the texture height of the outlet *h*_{tex},_{*out*} for each geometry. The color of each point represents the performance enhancement ratio (PER) and is scaled from one to the maximal PER. For every geometry, it can be observed that a small step on the left side of the texture with a height of 5-15 µm leads to leads to the best tribological performance. As previously discussed, the rectangle texture the best tribological performance. As previously discussed, the rectangle texture with a
the best tribological performance. As previously discussed, the rectangle texture with a constant width also causes the highest performance enhancement ratio (PER). Generally, for this convergent oil film gap, it can be observed that with an increasing texture area density $S_{textrm{tex,}A}$, the performance enhancement increases, and if the expansion of the texture allows, a local maximum exists.

Figure 6. Comparison between performance enhancement ratio, texture area density and texture height for different texture geometries: (a) rectangle constant width, (b) square, (c) rectangle variable width, (**d**) chevron, (**e**) equilateral triangle, (**f**) half hexagon, (**g**) hexagon, (**h**) half hexagon (inlet large) and (**i**) semicircle.

With the aid of the previously discussed data, the pitch angle *α*_{tex} for the best-performing texture geometries is calculated (cf. Table [2\)](#page-7-1). It can be observed that for textures where a local maximum of the PER exists, an optimal pitch angle *α*_{*tex*. Of about} shows where a local maximum of the texture, an optimal phen at t_{tx} , or t_{rx} , or t_{rx} , $0.52°$ to $0.67°$ exists, with the exception of the chevron-shaped one, which has an optimal pitch angle α_{tex} of 0.94[°].

To analyze the results of Figure [6](#page-7-0) in detail, the performance enhancement ratio (PER) over the texture height on the outlet side $h_{tex, out}$ and over the texture area density $S_{tex, A}$ is

plotted in Figure [7.](#page-8-0) In this figure, three horizontal axes are visible, where the blue axes are related to each other. The blue curves represent the influence of the texture area density $S_{tex, t}$. The texture height at the outlet side is kept constant at the value of $h_{tex, out}$, which achieved the highest performance enhancement ratio (PER). The purple curves visualize the dependency of *htex*.,*out* for the best-performing texture at its optimal texture area density *Stex*.,*A*. Compared with Figure [6,](#page-7-0) these graphs should quantitatively describe horizontal (blue curves) and vertical plots (purple curves) at the maximal PER for each geometry. For texture geometries with a pitch angle α_{tr} unequal to zero, where the texture area density $S_{tex, t}$ and texture volume density $S_{tex, t}$ = $V_{tex, t}$, V_0 differ, an additional *x*-axis is added to visualize this texture volume density S_{tr} , *V*. For the different rectangles and the square-shaped texture, a local maximum at a texture area density *Stex*.,*^A* of 69–75% exists. For the chevron-shaped geometry, the best tribological performance can be achieved at $S_{textrm{tex,}A} = 53\%$. All other geometries have the highest PERs at the highest texture area densities *Stex*.,*A*. The blue curve of the equilateral triangle and the semicircle texture are quite similar. Additionally, it can be observed that the different orientation of the half
hexagon influences the performance in the low region of $S_{tex, A}$ and with an increasing
density that both curves gradually approac hexagon influences the performance in the low region of *Stex*.,*^A* and with an increasing density that both curves gradually approach. The purple curves in Figure 7 depict the influence of the texture height on the outlet side $h_{tx.,\text{out}}$, and it can be observed that for all visualizations, a local maximum exists. This means that a small step on the outlet side
. improves the tribological performance. defice of the texture height on the outlet side h_{ℓ} , $_{\ell}$, $_{\ell}$ and it can be observed it visualizations, a local maximum exists. This means that a sma
proves the tribological performance.

Figure 7. Performing enhancement ratio over texture area density/texture height on the for different geometries: (**a**) rectangle constant width, (**b**) square, (**c**) rectangle variable width, (**d**) chevron, (**e**) equilateral triangle, (**f**) half hexagon, (**g**) hexagon, (**h**) half hexagon (inlet large) and (**i**) semicircle. semicircle. (**d**) chevron, (**e**) equilateral triangle, (**f**) half hexagon, (**g**) hexagon, (**h**) half hexagon (inlet large) and **d**equilateral hexagon,) **h**) **i**side for different geometries: (**a**) rectangle constant width, (**b**) square, (**c**) rectangle variable width, Figure 7. Performing enhancement ratio over texture area density/texture height on the outlet
side for different geometries: (**a**) rectangle constant width, (**b**) square, (**c**) rectangle variable width
(**d**) chevron, (**e**) (**i**) semicircle.

3.3. Pressure and Velocity Analyses of Best-Performing Geometries

In Figure [8,](#page-9-0) the pressure distribution of the best-performing geometries is visualized. The hydrodynamic pressure values are scaled to the same range. In contrast to the smooth geometry, the texture significantly increases the maximal pressure. The maximal pressure can be achieved with the hexagon-shaped geometry, but since this maximal pressure is concentrated on a smaller area compared to the rectangles and squares, the lifting force \rightarrow

 F_{lift} is lower than these geometries. On the inlet side of the hexagon-shaped texture, some regions with a pressure of less than 0 can be observed, indicating possible cavitation. It should be noted that as long as the relative pressure is not below the vapor pressure p_v , negative relative pressures are possible. For all other geometries presented in Figure [8,](#page-9-0) this could not be observed. In all geometries, it is noticeable that the region of maximal pressure is located at the outlet area of the texture, while for the untextured oil film gap, it pressure is located at the outlet area of the texture, while for the untextured oil film gap, is in the center. \mathbf{r} .

Figure 8. Pressure distribution of best-performing texture geometries. **Figure 8.** Pressure distribution of best-performing texture geometries.

The velocity field in the x–y direction is depicted in Figure 9. The slice at the position The velocity field in the x–y direction is depicted in Figure [9.](#page-10-0) The slice at the position of $z = 10$ m is used to calculate the glyphs in this x–y plane. All vectors are scaled to $\frac{1}{\sqrt{2}}$ and the color represents the magnitude of the magnitude of the velocity $\frac{1}{\sqrt{2}}$ and $\frac{1}{\sqrt{2}}$ and the same length, and the color represents the magnitude of the velocity $|\vec{u}|$. The gradient between the inlet and outlet sides of the geometry can be explained by the different heights, which lead to different shear rates and, consequently, to a different magnitude of velocity $|\vec{u}|$. In contrast to the smooth wedge, a significant increase in the flow out on the surfaces that are located perpendicular to the movement direction can be observed. At the textures' end on the left side, an increase in the magnitude of the velocity $|\vec{u}|$ is visible. In these regions, a saltus of the height field exists, caused by the different heights in the texture at regions, a saltus of the height field exists, caused by the different heights in the texture at regarding the shear rate. the outlet side $h_{textrm{text,out}}$. This decreasing oil film gap height results in an increasing velocity flow on each side is evaluated. In Figure 10, these results are presented for one presented for regarding the shear rate.

To describe the previously mentioned results of Figure 9 quantitatively, the volume flow on each side's surface is evaluated. In Figure [10,](#page-10-1) these results are presented for one specific texture height at the outlet side $h_{textrm{text,}out} = 10 \mu m$. On the left side, the incoming volume flow Q_{in} , and on the right side, the volume flow that is perpendicular to the movement direction Q_{side} , are depicted. The volume flow on the left outlet side can be calculated by subtracting Q_{side} two times from Q_{in} . In Figure [10a](#page-10-1), it can be observed that the performance enhancement ratio (PER) increases with the increasing inflowing volume \mathcal{L} exists, the PER increases with the intrinsic volume inflower with the inflower volume inflower volume inflower volume inflower volume in \mathcal{L}

flow *Qin* until the local maximum of PER is achieved. This behavior is followed by a decreasing PER over *Qin*. For geometries where no local maximum of the performance enhancement ratio (PER) exists, the PER increases with the increasing inflowing volume flow Q_{in} . These similar trends can also be detected for the volume flow perpendicular to the movement direction *Qside*. For the rectangle-shaped textures, a special performance can be noticed. The volume flow that is perpendicular to the movement direction Q_{side} increases to the maximal performance enhancement ratio (PER) and then decreases.

Figure 9. Velocity distribution of best-performing texture geometries in x-y plane at a z-coordinate of 10 µm. of 10 µm.

flow perpendicular to movement direction for $h_{tex, out} = 10$ m. Figure 10. Performance enhancement ratio over (a) inflowing volume flow and (b) outflowing volume

be achieved with a rectangle-shaped texture with a rectangle-shaped texture with a texture length of \mathcal{A} . **4. Discussion 4. Discussion**

In Figure [8](#page-9-0), it can be observed that the highest performance enhancement ratio can be achieved with a rectangle-shaped texture with a texture length of $a_{text} = 1.732$ mm and $\frac{1}{2}$ is shown $\frac{1700}{2}$ and $\frac{1700}{2}$ and $\frac{1700}{2}$ and $\frac{1}{2}$ become the best-performing texture is also $\frac{16}{2}$ best-performing texture is also $\frac{16}{2}$ become the best-performing texture is also a texture width of $b_{text} = 1.700$ mm. The square-shaped surface modification with the dimensions $a_{text} = b_{text} = 1.717$ mm leads to nearly the same performance enhancement ratio. It should be noted that the geometry of the best-performing texture is also quite similar to a square. Gherca et al. [\[15\]](#page-14-11) conducted simulations for rectangle-, triangle- and parabolic-shaped textures for a parallel lubricated contact and found that for textures with small inlet lengths, the rectangle textures provide the highest load-carrying capacity. In the current study, the texture is open at the inlet, corresponding to an inlet length of 0 mm, and similarly, the rectangle-shaped texture provides the highest performance enhancement ratio (PER). In [\[15\]](#page-14-11), the texture area density *Stex*.,*^A* is increased by adding an additional texture, but it was observed that with the increasing texture area density *Stex*.,*A*, the friction force

 $\overrightarrow{F}_{drag}$ decreases, as shown in Figure [5.](#page-6-1) Uddin et al. [\[17\]](#page-14-13) examined seven different texture geometries (circle, square, hexagon, octagon, triangle, ellipse and chevron) for a parallel slider and concluded that the square-shaped texture leads to the highest load-carrying capacity at a texture area density *Stex*.,*^A* of 50%. In this work, the best performance can be achieved with a rectangle-shaped texture, but its width and length are almost the same, which concludes that the geometry is nearly a square. The best performance in this study is achieved at higher texture area densities $S_{textrm{text},A}$, compared to [\[17\]](#page-14-13). These differences could potentially be explained by different numerical models and simulation parameters, like the dimension of the parallel oil film gap $(l_0 = b_0 = 100 \mu m$ and $h_0 = 1 \mu m$ in [\[17\]](#page-14-13)) and different positions of the texture. In [\[17,](#page-14-13)[18\]](#page-14-18), the influence of the orientations of the chevron- and triangle-shaped elements are also discussed, and it was observed that for both textures, the highest load-carrying capacity can be achieved if the wide side is oriented at the inlet side, justifying the orientation of the textures used in this study for the chevron and rectangle.

In general, all textures look similar to a Rayleigh step, which is already known in literature. Rahmani et al. [\[37\]](#page-15-4) optimized a Rayleigh step for a two-dimension parallel sliding bearing and concluded that the optimal length of the Rayleigh step is about 70% *l*0. Within this study, the optimal texture length for a best-performing texture, at about 87% l_0 , can be observed. It should be noted that, in this study, a finite convergent oil film gap is determined, compared to [\[37\]](#page-15-4).

Yu et al. [\[18\]](#page-14-18) analyzed the performances of circle-shaped, differently orientated triangle-shaped and ellipse-shaped textures. They found that as the texture area density *Stex*.,*^A* increases, the dimensionless average pressure initially rises to a local maximum before decreasing [\[18\]](#page-14-18). For the best-oriented ellipse- and rectangle-shaped textures, no local maximum was observed, as the interval of the texture area density *Stex*.,*^A* was defined between 3% and 30% [\[18\]](#page-14-18). The presence of a local maximum and a continuous increase in performance enhancement can also be seen in Figures 3 and 4 . However, in this study, higher texture area densities *Stex*.,*^A* were examined, compared to the work of Yu et al. [\[18\]](#page-14-18).

Ji et al. [\[20\]](#page-14-14) focused on parabola-, rectangle- and triangle-shaped textures in their publication, where the parabola and triangle describe the geometry of the bottom profile. They discovered that the rectangle-shaped texture achieved the highest load-carrying capacity at a textured fraction *ltex*./*l*⁰ of about 0.7 [\[20\]](#page-14-14). This value is close to the value (0.85) that yielded the best performance in this study.

However, the previously discussed publications analyzed the influence of different texture geometries for parallel sliding contact, in contrast to [\[21\]](#page-14-17), where the performance of eight different textures for a convergent oil film gap was analyzed. Wei et al. [\[21\]](#page-14-17) focused on dimples with a maximal dimension of 200 μ m and used more dimples for their simulation model. The effect of the texture area density *Stex*.,*^A* was only investigated for circle-shaped textures. The performance of the different texture geometries was analyzed for a constant number of equal dimples, causing different texture areas *Atex*. And, consequently, different *Stex*.,*^A* [\[21\]](#page-14-17). Nevertheless, the highest load-carrying capacity can be achieved for a squareshaped texture with 91 dimples [\[21\]](#page-14-17). Additionally, in [\[21\]](#page-14-17), the number of circle-shaped dimples varied between 15 and 91 dimples (which corresponds to a texture area density *Stex*.,*^A* of between approximately 2% and 11.4%) and concluded that a linear regression between the dimple number and dimensionless pressure exists [\[21\]](#page-14-17). The comparison between this solution and the result of Figure [4](#page-6-0) shows that in the region of low texture

area density $S_{textrm{tex},A}$, it seems that the lifting force $\overrightarrow{F}_{lift}$ is linearly dependent on the texture area density *Stex*.,*A*. With the increasing texture area density *Stex*.,*A*, this behavior definitely cannot be observed.

According to Grützmacher et al. [\[2\]](#page-13-1), providing additional volume flow is one possible working principle of textures. In Figure [10a](#page-10-1), it can be observed that this possible mechanism is also present in this study, as the performance enhancement ratio increases with the increasing inflowing volume flow Q_{in} . However, it is important to note that providing additional volume flow only at the inlet is not sufficient, as the performance enhancement ratio (PER) can also decrease with the increasing inflowing volume flow *Qin*. Kumar et al. [\[19\]](#page-14-19) found that for specific textures, there is a local maximum load-carrying capacity over the texture height h_{trx} and they also analyzed the flow rate, which increases with the increasing texture height *htex*. Therefore, a similar performance to the one presented in this study could be observed by Kumar et al. [\[19\]](#page-14-19).

In general, the lifting force $\overrightarrow{F}_{lift}$ of an infinite, expanded, convergent oil film gap, where no fluid is emitted on the surfaces perpendicular to the movement direction, is higher compared to a finite one [\[35\]](#page-15-2). Nevertheless, in Figure [10b](#page-10-1), for a rectangle-shaped texture, it can be observed that the performance enhancement ratio (PER) increases with the increasing volume flow perpendicular to the movement direction. It appears that after achieving the highest performance enhancement ratio (PER), it then decreases.

Within this study, the tribological performance of open textures at the inlet was analyzed. Consequently, a modified chevron texture was used in this work. Figure [5](#page-6-1) presented that in the region of the mid-texture area densities $S_{tex, A}$, the drag force $\overrightarrow{F}_{drag}$ of the chevron-shaped texture was significantly lower compared to the other geometries, with a maximal relative reduction of approximately 18% in friction. Although Morris et al. [\[38\]](#page-15-5) conducted simulations for a convergent oil film gap with multiple chevron textures, they published a maximal friction reduction of about 15%, which is similar to the value achieved in this study.

The influence of the bottom surface profile of a texture is discussed by Uddin et al. [\[17\]](#page-14-13), and they showed that this profile significantly influences the load-carrying capacity. In contrast to this work, Uddin et al. [\[17\]](#page-14-13) used bottom surface profiles, such as a constant height for a single or double wedge-shaped texture for the squared-shaped texture. This main conclusion is also observed in this study, where in Figures [6](#page-7-0) and [7,](#page-8-0) it is seen that a small step of the texture on the outlet side improves the tribological performance.

5. Conclusions

Within this study, a numerical model was implemented to investigate the influence of nine different texture geometries on different texture area densities *Stex*.,*A*. In comparison to the existing studies, this work examines the performance of open textures at the inlet for a convergent oil film gap. Additionally, the influence of the pitch angle *αtex*. was analyzed. The following conclusions are depicted in Figure [11](#page-13-2) and can be summarized as follows:

- Depending on the texture area density *Stex*.,*A*, different texture geometries enhance the tribological performance the most (cf. Figure [11\)](#page-13-2).
- The rectangle texture with a variable width enhances the tribological performance the most over a wide range of texture area densities $S_{text, t}$ (cf. example for $S_{text, t}$ ₂ = 27% and $h_{tex, out} = 30 \mu m$ in Figure [11\)](#page-13-2).
- The best performance can be achieved with a rectangle-shaped texture with a constant width (cf. Figure [11\)](#page-13-2). The square-shaped texture also leads to almost the same performance (cf. Figure [11](#page-13-2) for the best-performing texture).
- For rectangle-, square- and chevron-shaped elements, a local maximum of the performance enhancement ratio (PER) exists. For all other geometries, simulations had to be aborted before reaching a maximum due to the requirement that the texture geometry cannot protrude the convergent oil film gap (cf. Figure [11\)](#page-13-2).
- The drag force $\overrightarrow{F}_{drag}$ decreases with the increasing texture area density $S_{textrm{.},A}$.
- A small step of the texture at the outlet side of the texture between 10 μ m and 15 μ m, corresponding to a pitch angle of the texture *αtex*. between 0.5◦ and 1.8◦ , improves the tribological performance (cf. Figure [11\)](#page-13-2).
- The hexagon-shaped texture leads to the highest pressure, but as it is located in a smaller region, compared to other texture geometries, the lifting forces $\overrightarrow{F}_{lift}$ of the rectangle- and square-shaped textures are higher.
	- Providing an additional volume flow at the inlet *Qin* does not guarantee an improvement in tribological performance.
	- Compared to a smooth convergent oil film gap, a significant increase in the volume Compared to a smooth convergent oil film gap, a significant increase in the volume flow can be observed (cf. Figure 11). flow can be observed (cf. Figure [11\)](#page-13-2).

Figure 11. Summary of results. **Figure 11.** Summary of results.

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